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Eu³⁺-doped β-Ga₂O₃ nanophosphors: annealing effect, electronic structure and optical spectroscopy[†]

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A comprehensive survey of electronic structure and optical properties of rare-earth ions-doped semiconductor is of vital importance for their potential applications. In this work, Eu^{3+} -doped β -Ga₂O₃ nanocrystals were synthesized *via* a combustion method. The evolution of the optical properties of nanophosphors with increasing the annealing temperature was investigated in detail by means of excitation and emission spectra at room temperature and 10 K. Eu³⁺ ions were proved to be incorporated into the crystal lattice of the β -Ga₂O₃ phase after annealing the as-prepared nanoparticles at 1100 °C. It was observed that the substitution of Eu³⁺ for Ga³⁺ occurred at merely single site, in spite of two crystallographically nonequivalent sites of Ga^{3+} in β -Ga₂O₃. Spectroscopic evidence corroborated and clarified the local symmetry of C_s for Eu³⁺ at this single site. From the high-resolution excitation and emission spectra, 71 crystal-field levels of Eu^{3+} in β -Ga₂O₃ were identified and analyzed in terms of 19 freely varied free-ions and crystal-field parameters based on $C_{\rm s}$ symmetry. The standard deviation of the final fitting is as low as 12.9 cm^{-1} , indicating an excellent agreement between experimental and calculated energy levels. The temperature-dependent luminescence dynamics of the ${}^{5}D_{0}$ multiplet for Eu³⁺ in β -Ga₂O₃ phosphors has also been revealed for the first time from 10 to 300 K.

Introduction 1.

Rare-earth (RE)-doped semiconductor nanocrystals (NCs) have attracted considerable attention in the past decade for their ability to tailor the optical properties via size control and to achieve efficient RE luminescence sensitized by exciton recombination in the host. These unique optical properties enable them to have potential applications in areas as diverse as full color display,^{1,2} biolabels,³ and phosphors.^{4–7} Gallium oxide (Ga₂O₃) has five crystal structures and β -Ga₂O₃ is the most stable phase, which is a semiconductor with a wide band gap of ~4.8 eV.^{8,9} The structure of β -Ga₂O₃ is monoclinic with a space group of C2/m, and Ga^{3+} ions occupy two crystallographic sites, namely tetrahedral and octahedral, respectively.¹⁰ β-Ga₂O₃ has been reported as a promising material for applications in the fields such as high temperature gas sensor,^{11,12} catalyst,¹³ and optoelectronic devices.¹⁴ Great efforts have been made to investigate the optical properties of Ga₂O₃, including the origin of the self-activated luminescence,^{15–18} the emission of the impurity nitrogen^{19,20} and the optical properties of various nanostructured materials such as nanowires²¹ and nanobelts.²²

Recently it has been realized that β -Ga₂O₃ is also a good host for RE ions due to their high thermal and chemical stability and a wide range of optical transparency. The wide band gap of the host may allow us to improve the luminescence efficiency of RE emissions.²³ The large refraction index of β -Ga₂O₃ (1.85–1.91) combined with the RE luminescence makes RE-doped B-Ga₂O₃ attractive for waveguiding applications.²⁴ Up to now, the visible and infrared luminescence of Er^{3+} in β -Ga₂O₃ have been occasionally reported with either photon or electron excitation.^{14,24–27} Dy³⁺-doped β-Ga₂O₃ synthesized with various morphologies showed a morphology-dependent optical properties,²⁸ and efficient host-to-Dy³⁺ energy transfer (ET).^{28,29} The codoping of Li⁺ was proved to be able to enhance the photoluminescence (PL) intensity of Dy^{3+} in β -Ga₂O₃.³⁰ It is expected that, by integrating the distinct optical properties of Eu³⁺, Eu³⁺-doped β -Ga₂O₃ is of particular interest for bioprobes, lighting and displays applications. The electroluminescence devices based on Eu³⁺-doped Ga₂O₃ thin films were demonstrated with relatively low threshold voltage.31-34 Eu3+-doped Ga2O3 NCs and phosphors were also synthesized by a variety of

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[†] Electronic supplementary information (ESI) available: TEM and SAED images of the sample annealed at 650 °C; RT emission spectrum of 0.1 at% Eu³⁺ doped β -Ga₂O₃ annealed at 650 °C upon excitation at 285 nm; RT emission spectra of the sample annealed at 1000 °C before and after washing with diluted HNO3 upon excitation at 285 nm. See DOI: 10.1039/c0cp02520h

methods and their PL properties have been characterized preliminarily.^{35–39} However, the Eu³⁺ emission and excitation spectra presented in those works showed a broadband behavior rather than sharp transition lines that were typical of Eu³⁺ in a crystalline environment, indicating that Eu³⁺ ions might be located at the surface or close to the surface sites instead of entering the crystal lattice of β -Ga₂O₃. To date, the electronic structure and detailed optical properties, such as luminescence dynamics and site symmetry analysis of Eu³⁺ ions in the β -Ga₂O₃ lattice, are still lacking. Therefore, further systematical investigation of the optical properties of Eu³⁺ in β -Ga₂O₃ is of vital importance for their future applications.

In this work, we will present the synthesis of Eu^{3+} -doped β -Ga₂O₃ NCs *via* a simple combustion method. The correlation between the optical properties and annealing conditions, local site symmetry and PL dynamics of Eu^{3+} in β -Ga₂O₃ NCs will be investigated in detail. Spectroscopic evidence will be provided for the incorporation of Eu^{3+} into the β -Ga₂O₃ lattice, and crystal-field (CF) analysis for the observed energy levels in this new kind of phosphors will be carried out for the first time.

2. Experimental details

2.1 Nanocrystal synthesis

Eu³⁺-doped β -Ga₂O₃ NCs were synthesized by a combustion method reported by Mahalingam *et al.*⁴⁰ The Ga₂O₃ (AR), Eu(NO₃)₃·6H₂O (AR) and glycine (AR) were used as raw chemicals. The synthesis procedure for 1 at% Eu³⁺-doped β -Ga₂O₃ samples was briefed as follows. Firstly, 0.3711 g Ga₂O₃ was dissolved in diluted nitric acid and the solution was evaporated at 70 °C until Ga(NO₃)₃·xH₂O was obtained. Then 0.0178 g Eu(NO₃)₃·6H₂O, 0.3603 g glycine and 25 mL distilled water were added. The resultant solution was stirred for 10 h and then evaporated at 120 °C in an oven. When a transparent residue was formed the temperature was increased to 220 °C and the combustion reaction took place. The as-prepared products were then annealed under various conditions in air, that is, 650 °C for 5 h, 900 °C for 5 h, 1000 °C for 10 h and 1100 °C for 24 h, respectively.

2.2 Characterization

The phase identification of the samples was performed by powder X-ray diffraction (XRD) using a Miniflex II diffractometer with Cu K α 1 radiation ($\lambda = 0.154$ nm). The morphologies of the NCs were characterized by a JEOL-2010 transmission electron microscopy (TEM). The excitation and emission spectra and transient decays were measured using an Edinburgh Instrument FLS920 spectrometer equipped with both continuous (450 W) and microsecond pulsed xenon (Xe) lamps. For low temperature (10 K) experiments, the sample was mounted on an optical cryostat (10–350 K, DE202, Advanced Research Systems). For laser excited PL measurements, a frequency doubling Ti:sapphire laser (700–1000 nm, pulse width ≤ 1.5 ps, Tsunami, Spectra Physics) was used for excitation. All the spectra were corrected for the instrument response.

3. Results and discussion

3.1 Structural and morphology characterization

The XRD pattern of the 1 at% Eu^{3+} -doped sample annealed at 650 °C was shown in Fig. 1. It can be seen that the pattern is in line with the C2/m space group of β -Ga₂O₃ (JCPDS NO. 43-1012). This is consistent with the result that the β phase can be formed under the annealing temperature higher than 600 °C.^{29,41} However, the barely resolved diffraction peaks indicate very small size of NCs. TEM images of this sample show that the NCs are aggregated but clear crystalline lattice fringes can be observed. The selected-area electron diffraction (SAED) pattern exhibits a polycrystalline nature and the diffraction rings can be well indexed to the (002), (111), $(\bar{1}12)$ and (710) planes of β -Ga₂O₃ (Fig. S1 in the ESI[†]). The clear crystalline lattice fringes and diffraction rings suggest that the samples annealed at 650 °C were well crystallized. The XRD patterns of 1 at% Eu³⁺-doped samples annealed at higher temperatures are also shown in Fig. 1 for comparison. Obviously, the NCs grow larger with higher annealing temperature and longer annealing time. The average diameters estimated by Debye-Scherrer's formula are 5, 20, 30 and 45 nm for samples annealed at 650, 900, 1000 and 1100 $^\circ C$, respectively.

3.2 Excitation and emission spectra

Fig. 2 shows the room temperature (RT) excitation and emission spectra of the 1 at% Eu³⁺-doped sample annealed at 650 °C. When excited at 285 nm, as shown in Fig. 2(a), all the emissions were originated from the ⁵D₀ multiplet of Eu³⁺. No emissions from the ⁵D₁ and ⁵D₂ multiplets were observed, even in 0.1 at% Eu³⁺-doped counterparts (Fig. S2 in the ESI[†]), in which the concentration quenching can be neglected. This suggests an efficient multiphonon relaxation from the upper exited states to ⁵D₀. When monitored the ⁵D₀ \rightarrow ⁷F₂ emission, the excitation spectrum in a range of 230–550 nm was shown in Fig. 2(b). In addition to the sharp 4f-shell inner transitions from ⁷F₀ to ⁵D_{1,2,3,4} and ⁵L₆ of Eu³⁺, a strong and broad excitation band centered at 285 nm with a full width at

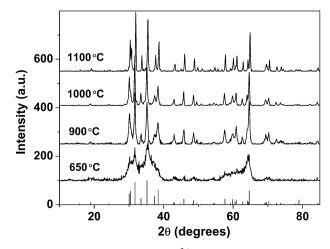


Fig. 1 XRD patterns of 1 at% Eu^{3+} -doped β -Ga₂O₃ annealed at various conditions. The bars represent the standard XRD data of β -Ga₂O₃ (JCPDS NO. 43-1012).

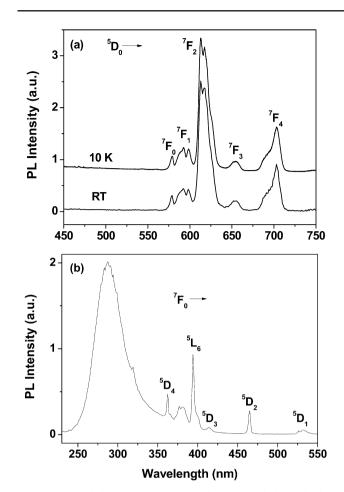


Fig. 2 (a) Emission spectra at RT and 10 K, and (b) excitation spectrum at RT for the 1 at% Eu³⁺-doped sample annealed at 650 °C. The ⁵D₀ \rightarrow ⁷F₂ emission was monitored in the excitation spectrum. The emission spectrum was measured upon excitation at 285 nm.

half maximum (FWHM) of 40 nm was observed. It was reported that in Dy^{3+} -doped β -Ga₂O₃ NCs the Dy^{3+} luminescence can be sensitized by the host with a broad excitation band centered at 257 nm, corresponding to the ~4.8 eV band gap of β -Ga₂O₃.²⁹ However, in this case, the energy of the excitation peak is lower than the band gap of β -Ga₂O₃. The possible reasons for the red shift of this excitation band will be discussed later. Fig. 2(a) also shows the 10 K emission spectra of the sample annealed at 650 °C for comparison. As we can see, no resolved emission lines between the CF levels of Eu³⁺ can be observed at 10 K. The emission spectra at 10 K and RT remain essentially unchanged. This phenomenon means that the spectra were broadened inhomogeneously, in other words, these emissions may arise mainly from the Eu³⁺ ions that occupied a surface or near surface site.

To investigate the annealing effect on the optical properties of Eu^{3+} in β -Ga₂O₃, the 10 K emission spectra of 1 at% Eu^{3+} -doped samples annealed at 900, 1000, and 1100 °C were measured and shown in Fig. 3(a), respectively. It shows clearly that, different from the sample annealed at 900 °C, the other two counterparts exhibit sharp and well-resolved transition lines, revealing that more Eu^{3+} ions were incorporated into the crystal lattices as the annealing temperature increased

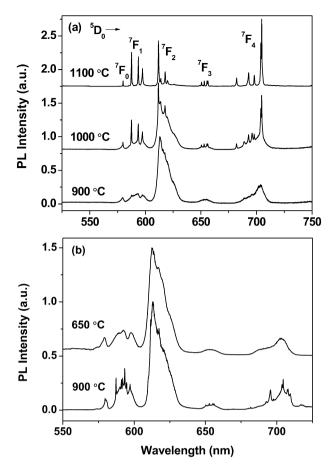


Fig. 3 (a) The 10 K emission spectra upon excitation at ~ 270 nm with a Xe lamp for the samples annealed at 900, 1000 and 1100 °C, respectively. (b) The 10 K emission spectra upon laser excitation at 394 nm for the samples annealed at 650 and 900 °C, respectively.

gradually. The absence of sharp lines for the sample annealed at 900 °C is probably due to the fact that only a small portion of Eu^{3+} ions was in the NC lattices and the related emission is too weak to be observed under Xe lamp excitation. To prove this, the emission spectra of the samples annealed at 650 and 900 °C were measured at 10 K using a frequency doubling Ti:sapphire laser at 394 nm as the pump source. As shown in Fig. 3(b), no sharp transition lines were observed for the sample annealed at 650 °C even under laser excitation, suggesting that much less Eu³⁺ ions in this sample entered into the crystal lattice. By contrast, sharp transition lines of ${\rm Eu}^{3\,+}$ emerged for the sample annealed at 900 $^{\circ}{\rm C},$ verifying that a small portion of Eu³⁺ ions was indeed incorporated into the crystal lattice. For NCs, the ratio of surface-to-volume increases with decreasing particle size. Consequently more Eu³⁺ ions are located close to the surface in smaller NCs. Due to more serious structural defects near the surface, those Eu³⁺ ions may experience various CF environments and their PL spectra will be broadened inhomogeneously. With the NC growth, the portion of the Eu³⁺ ions on the surface or near the surface decreases that gives rise to much sharper PL emission lines. It is worthy of noting that only broad and unresolved emission bands analogous to that of the sample annealed at 650 °C (Fig. 2) were observed at RT for Eu³⁺-doped β -Ga₂O₃

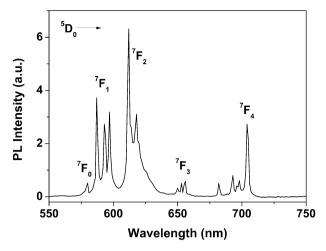


Fig. 4 RT emission spectrum upon excitation at 266 nm for the sample annealed at 1100 °C.

previously reported.^{31,33,35–39,42} In sharp contrast, much sharper transition lines of Eu^{3+} (with a FWHM of ~1.5 nm) can be observed at RT for the sample annealed at 1100 °C (Fig. 4). This further confirms the successful incorporation of Eu³⁺ ions into the β -Ga₂O₃ lattice. Note that the RT and 10 K emission lines of the sample annealed at 1100 °C are markedly different from those of the Eu₂O₃ polycrystalline powders in terms of peak positions and shapes,^{43,44} therefore the formation of the Eu₂O₃ clusters or impurities in the sample can be ruled out. To verify the above assumption that the broad emissions arise mainly from Eu³⁺ ions close to the surface. The samples annealed at 650 and 1000 °C were intentionally washed with diluted HNO₃ to investigate the surface effects on their PL spectra. After washing with HNO₃, the emission spectrum of the sample annealed at 1000 °C was indeed improved, sharper than that measured before washing (Fig. S3 in the ESI[†]). For the sample annealed at 650 °C, the emission spectrum remains essentially unchanged before and after washing. This is also reasonable since few Eu^{3+} ions were in the lattice of β -Ga₂O₃, therefore washing the NCs with HNO₃ does not change the spectrum.

Fig. 5 compares the 10 K excitation spectra of the samples annealed at 650, 900, 1000 and 1100 °C by monitoring the ${}^{5}D_{0} \rightarrow {}^{7}F_{2}$ emission. With increasing the annealing temperature, the peak of the broad excitation band is blue shifted from 285 to 266 nm, which is close to the \sim 4.8 eV band gap of β -Ga₂O₃. Simultaneously, the FWHM of the band decreases with higher annealing temperature. Previously, similar broad excitation bands peaked at very different wavelengths were observed in Eu³⁺-doped β -Ga₂O₃, for example, ~305 nm for the nanophosphors synthesized by a sol-gel method,^{38,39} \sim 280 nm for bulk crystals synthesized by a solid state reaction method,³⁸ ~ 270 nm for thin films prepared by chemical bath deposition,⁴² and ~ 257 nm for thin films prepared by pulsed laser deposition.³⁴ For laser deposited films, the excitation band at ~ 257 nm was ascribed to the band gap transition of the host, while those of other samples were assigned to the $Eu^{3+}-O^{2-}$ charge transfer transition. For Dy^{3+} and Er^{3+} -doped β -Ga₂O₃, the broad excitation bands with peaks at ~255 nm were also observed when monitoring the RE emission and

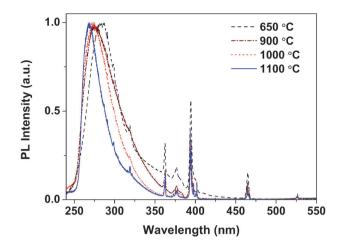


Fig. 5 The 10 K excitation spectra by monitoring ${}^{5}D_{0} \rightarrow {}^{7}F_{2}$ emission of Eu³⁺ for the samples annealed at 650, 900, 1000 and 1100 °C, respectively.

considered as the band gap transition of the host.^{25,28,29} The polarized absorption or excitation spectra of β -Ga₂O₃ single crystals were measured and the absorption band edges were found to be dependent on the electric field orientation (E) of the excitation light due to the anisotropy of the monoclinic structure. Binet and Gourier¹⁶ reported the absorption edges located at 4.7 and 4.6 eV for E/b and $E \perp b$ (b represents the two fold crystallographic axis of β -Ga₂O₃), respectively. Ueda et al.⁹ evidenced that the absorption band edges were 4.9 and 4.7 eV for E//b and $E \perp b$, respectively. Moreover, the band gap widening was observed with the increase of the carrier concentration.⁴⁵ Therefore, the band gap of β-Ga₂O₃ may differ under different synthesis conditions such as the growth atmosphere, annealing time and impurity doping. The excitation band at 266 nm that we observed is falling in the range of the reported band gap values and thus can be attributed to the band gap transition of the host.^{8,9,16,46} The blue shifting of the excitation peak is very likely owing to the decrease of the defect concentration in β -Ga₂O₃ annealed at higher temperatures, since the defect (oxygen or gallium vacancies) excitation bands with energies slightly below the band gap were observed in β -Ga₂O₃.^{16,46} As shown in Fig. 5, the excitation band at 266 nm is much stronger than that of the 4f-4f transitions of Eu³⁺, suggesting an efficient hostto-Eu³⁺ ET.

3.3 Local site symmetry of Eu³⁺

The following site symmetry analysis is based on the sample annealed at 1100 °C, in which most Eu³⁺ ions were proved to reside in the crystal lattice as discussed above. It is well-known that the ${}^{5}D_{0} \rightarrow {}^{7}F_{2}$ transition of the Eu³⁺ ions is of electric-dipole (ED) nature and hypersensitive to the site symmetry but the ${}^{5}D_{0} \rightarrow {}^{7}F_{1}$ transition is of magnetic-dipole (MD) and insensitive to the site symmetry. According to the selection rules of the EU transition, the ${}^{5}D_{0} \rightarrow {}^{7}F_{2}$ transition is allowed only when the Eu³⁺ ions occupy a site without an inversion center. As shown in Fig. 3(a), the ratio of the integrated PL intensities of the ${}^{5}D_{0} \rightarrow {}^{7}F_{2}$ and ${}^{5}D_{0} \rightarrow {}^{7}F_{1}$ transitions is 1.4 for the sample annealed at 1100 °C. Therefore, the Eu³⁺

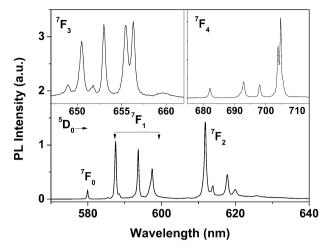


Fig. 6 High-resolution emission spectra at 10 K upon band gap excitation for the sample annealed at 1100 °C.

ions most probably occupy a site without an inversion center. Moreover, on the basis of the selection rules of ED and MD transitions, the allowed ${}^{5}D_{0} \rightarrow {}^{7}F_{J}$ (J = 0, 1, 2, 3, 4, 5, and 6) transition lines in 32 crystallographic point groups can be obtained.⁴⁷ By comparing the observed transition lines with the theoretical numbers, we can assign the possible Eu^{3+} site symmetries from the measured 10 K emission spectrum. Fig. 6 shows the enlarged 10 K emission spectra of the sample annealed at 1100 °C. The emission spectra were collected upon excitation above the band gap of β -Ga₂O₃, therefore all the Eu³⁺ ions will be excited through host-to-Eu³⁺ ET provided that Eu³⁺ ions occupy multiple sites in the crystal lattices. The numbers of the observed transition lines of the ${}^{5}D_{0} \rightarrow {}^{7}F_{0}$, ${}^{7}F_{1}$, ${}^{7}F_{2}$, ${}^{7}F_{3}$ and ${}^{7}F_{4}$ transitions are 1, 3, 5, 7 and 5, respectively. We further measured the luminescence decay curves at 10 K by monitoring the four emission lines of the ${}^{5}D_{0} \rightarrow {}^{7}F_{0}$, ${}^{7}F_{1}$ transitions, respectively. The decay curves are exactly the same, verifying that these emissions were originated from the same Eu³⁺ resided in a single lattice site. Based on the above spectroscopic evidence, the highest local site symmetry of Eu^{3+} is deduced to be C_8 or C_2 .

It should be noted that the Ga³⁺ ions occupy two crystallographic sites in β -Ga₂O₃, tetrahedral (coordinated with four oxygen ions) and octahedral (coordinated with six oxygen ions). In several papers concerning the local site symmetry of RE ions in β -Ga₂O₃, these two sites were assigned with T_d (tetrahedral site) and O_h (octahedral site) symmetries, respectively.^{29,30,36,37} However, according to the crystal structure of β -Ga₂O₃,¹⁰ the tetrahedron and octahedron are not regular but distorted and the real point-group of Ga³⁺ sites should be lower than T_d and O_h . In fact, both kinds of Ga^{3+} ions occupy 4*i* positions with the same site symmetry of C_s in accordance with the C2/m space group.¹⁰ The single crystal NMR spectroscopy of β -Ga₂O₃ also verified the local mirror-plane symmetry of these two gallium sites.⁴⁸ Most importantly, the C_s symmetry of Ga³⁺ is also consistent with the site symmetry deduced by the PL spectra of Eu³⁺ in this work. Because of the same symmetries for both crystallographic sites, it's difficult to determine the exact site of Ga³⁺ that the Eu³⁺ ions substitute for. Nevertheless, the ionic radii of the Ga³⁺

ions are 0.047 and 0.062 nm for tetrahedral and octahedral coordination, respectively.^{29,49} Taking into account the ionic radius of the Eu³⁺ ions (0.095 nm), the distorted octahedral site should be more suitable to accommodate Eu³⁺ ions. This is also in excellent agreement with foregoing spectral assignment because only a single lattice site of Eu³⁺ was observed for the sample annealed at 1100 °C. The electron paramagnetic resonance (EPR) measurements of Er³⁺-doped β -Ga₂O₃ single crystal also demonstrated that the incorporation of Er³⁺ (ionic radius of 0.088 nm) occurred at a single crystallographic site.²⁷

3.4 Crystal-field analysis

Generally, the CF interaction is relatively weak compared with electrostatic and spin–orbit coupling because the partially filled 4f shell is shielded by the filled 5s and 5p orbitals. The commonly used effective operator Hamiltonian is

$$H = H_{\rm FI} + H_{\rm CF},\tag{1}$$

Where the free-ion (FI) Hamiltonian can be expressed as:

$$H_{\rm FI} = E_{\rm avg} + \sum_{k=2,4,6} F^k f_k + \zeta_f A_{\rm SO} + \alpha L(L+1) + \beta G(R_2) + \gamma G(R_7)$$

+
$$\sum_{i=2,3,4,6,7,8} T^i t_i + \sum_{h=0,2,4} M^h m_h + \sum_{f=2,4,6} P^f p_f,$$
(2)

The physical meaning of these FI parameters has been described by Crosswhite and Carnall *et al.*^{50,51} The single-particle CF Hamiltonian is expressed in Wybourne's notation,⁵²

$$H_{\rm CF} = \sum_{k,q} \operatorname{Re}B_q^k [C_q^k + (-1)^q C_{-q}^k] + i \operatorname{Im}B_q^k [C_q^k - (-1)^q C_{-q}^k]$$
(3)

For Eu³⁺ ion at the C_s site, kq = 20, 22, 40, 42, 44, 60, 62, 64 and 66, with a total number of 15 CF parameters. A reflection plane is introduced to make the imaginary part of B_2^2 equal to zero, which reduces the total number of independent CF parameters from 15 to 14.

From the 10 K excitation and emission spectra of the sample annealed at 1100 °C, 71 CF levels of Eu³⁺ in β -Ga₂O₃ have been identified. The CF levels of Eu³⁺ were fitted at C_s symmetry using the f-shell empirical programs from Reid.53 The detailed fitting procedure is similar to that reported by Liu and Chen.54 The FI parameters of Eu^{3+} : LaF₃⁵¹ and CF parameters of Eu^{3+} : Gd₂O₃⁵⁴ were used as initial values for the fitting. The standard deviation of the final fit is 12.9 cm⁻¹, showing a good agreement between experimental and calculated values. Table 1 compares the experimental and fitted CF levels below $34\,000$ cm⁻¹. Table 2 lists the obtained FI and CF parameters. The derived FI parameters of Eu^{3+} in β -Ga₂O₃ are close to those in In₂O₃⁶ but CF parameters differ appreciably in magnitude. Particularly, the B_0^2 , Re B_4^4 , Im B_4^4 , B_0^6 , Re B_2^6 , Im B_4^6 , Im B_4^6 , Re B_6^6 , and Im B_6^6 values have opposite signs, indicating a very different CF environment experienced by Eu^{3+} in β -Ga₂O₃.

Table 1 CF levels of Eu^{3+} at the C_s site of β -Ga₂O₃ at 10 K

	Energy/cm ⁻¹			Energy/cm ⁻¹			Energy/cm ⁻¹			Energy/cm ⁻¹			$\mathrm{Energy}/\mathrm{cm}^{-1}$	
SLJ	Exp.	Fit	SLJ	Exp.	Fit	SLJ	Exp.	Fit	SLJ	Exp.	Fit	SLJ	Exp.	Fit
$^{7}F_{0}$	0	4		21 510	21 498		26483	26471			27 744		_	31 290
${}^{7}F_{1}$	223	242			21 526		_	26484		_	27 7 51		31 299	31 301
- 1	401	402	$^{5}D_{3}$	24 284	24 273		_	26495		_	27834		_	31 31 3
	505	515	5	_	24 293		26 511	26 505			27 838			31 330
${}^{7}F_{2}$	899	887		24 3 25	24 314		_	26 521			27 880			31 349
	955	943		_	24 335			26 529			27 883			31 355
	1058	1061			24 345			26 546			27 931			31 368
	1115	1103		_	24 356		_	26 548		_	27 964		31 377	31 389
	1265	1264			24 372			26 563			27 988		_	31 391
${}^{7}F_{3}$	1836	1845	⁵ L ₆		24 7 58			26 572			28 038		_	31 408
1 3	1872	1858	20		24 772		_	26 573		_	28 044			31 421
	1902	1893		_	24 833		_	26 587		_	28 080			31 444
	1930	1933		24876	24 878		26617	26 612		_	28 087			31 469
	1986	1983			24 921			26 620			28 101		_	31 472
	2007	1990		24963	24 9 34			26 668		_	28 101			31 473
	2086	2089			24 978		_	26 677		_	28 120		_	31 491
⁷ F ₄	2584	2599		25107	25 106		_	26713		_	28 120			31 494
	2504	2792		25 107	25 209			26 721			28 127		_	31 504
	2812	2814		25 253	25 257			26 724		_	28 174		_	31 539
	2918	2913		25255	25 289		_	26 741		_	28 180		_	31 567
	2918	2913		25 323	25 349		_	26 744		_	28 213		_	31 570
	3038	3033		25 400	25 370		_	26 744		_	28 213		_	31 570
	3054	3057	${}^{5}G_{2,3}$		25 800		_	26 776		_	28 317		31 596	31 586
	3034	3130	${}^{5}G_{4,5}$	_	25 869		_	26 788		_	28 327			31 621
		3204	${}^{5}G_{6}$	_	25 871			26 799		_	28 431		_	31 649
${}^{7}F_{5}$	_	3741	⁵ L ₇	_	25 892		26817	26 805		_	28 455		31 676	31 679
F ₅	_	3745	L_7	25 900	25 892	⁵ L ₈		26 933		_	28 541			31 690
	_	3881		23 900	25 927	L_8	_	26 9 3 3		_	28 566		_	31 696
	_	3957		25947	25 927		_	26 949		_	28 500 28 575		_	31 722
	_	3991		25947	25 947		_	26972		_	28 575 28 594		_	31722
	_	3991		25994	26 000		27 020	27 033		_	28 594		_	31761
	_	4024		23 994	26 000		27020	27 033		_	28 680		_	31 701
	_	4024 4106		_	26 0 5 5		_	27 034 27 089		_	28 090		_	31 809
	_	4100			26 0 3 3		_	27 089		_	28 778			31809
		4203		26123	26118			27 094			28 778		—	31834
		4203		20123				27 188		_	28 791	${}^{3}P_{0}$	_	
$^{7}F_{6}$	_	4271 4846			26 150 26 170		27 218	27 188	⁵ H _{3,4}		28 795 30 869	${}^{5}F_{2,3}$		32 366 32 854
г ₆	_	4840		26 199	26 207		27 218	27 199 27 269	п _{3,4} 511		30 809	г _{2,3}	—	32 834
	_	4838		20199	26 207		21210	27 209	⁵ H _{5,6} ⁵ H ₇		30 881		—	32 8 9 5
	_	4933					_	27 290 27 316	Π7		30 909		—	32 893
		5037		26 247	26 236 26 242		27 322	27 310		_	30 930		32 960	32 948
	_			20247	26 242 26 258			27 332			30 949 30 959		52 900	
		5060		26 288						30 979				32967
		5221		20200	26 281	$^{5}D_{4}$		27 349		50979	30 962		33 014	33 015
		5235		_	26 295	51 51	_	27 472		_	30 978		_	33 031
		5286			26 295	⁵ L _{9,10}		27 499 27 528			31 034		22 102	33 050
		5316			26349		27 533			21.075	31 037		33 102	33 104
	_	5327		_	26355			27 548		31075	31 075			33 162
	—	5462			26359			27 564			31 099	5 _E		33 194
${}^{5}D_{0}$	17244	5463		26 285	26367		27 596	27 574			31 131	${}^{5}F_{1}$	—	33 324
⁵ D	17244	17 232		26385	26 397		27 586	27 590			31 162		—	33 343
$^{5}D_{1}$	18975	18959			26 402		27(17	27 609		—	31 186	5 _E		33 356
	19 008	19012			26 422		27 617	27 629			31 205	${}^{5}F_{4}$	_	33 373
5	19 033	19053			26434		27 647	27 643			31 213			33 397
⁵ D ₂	21 436	21 445			26 436			27 644			31 229			33 402
	21 450	21 464		26455	26 4 50			27 696			31 256		33 445	33 462
	21 468	21 478			26 468		27 693	27 702		_	31 285			

The scalar CF strength (S) that reflects the overall CF interaction in the crystal can be calculated using Chang's definition:⁵⁵

$$S = \left\{ \frac{1}{3} \sum_{k=2,4,6} \frac{1}{2k+1} \left[|B_0^k|^2 + 2 \sum_{q>0} \left(|\operatorname{Re}B_q^k|^2 + |\operatorname{Im}B_q^k|^2 \right) \right] \right\}^{1/2}$$
(4)

the calculated value of S is 546 cm⁻¹ for Eu³⁺ : β -Ga₂O₃, which is smaller than those of the cubic phase Eu³⁺ : Y₂O₃

(673 cm⁻¹),^{56,57} Eu³⁺ : Lu₂O₃ (718 cm⁻¹)^{58,59} and Eu³⁺ : In₂O₃ (790 cm⁻¹)⁶ with C_2 symmetry but larger than that of YAlO₃ (464 cm⁻¹)⁶⁰ with C_s symmetry. It was found that the CF strength of Eu³⁺ decreases with increasing ionic radius of the host cations for the M₂O₃ series (M = In, Lu, Y and Gd).^{6,61} However, the Eu³⁺-doped β-Ga₂O₃ doesn't obey this law albeit the ionic radius of Ga³⁺ is smaller than that of In³⁺. The possible reason is that the crystal structure and site symmetry of Eu³⁺ in β-Ga₂O₃ is different from those in M₂O₃ series. In fact,

Table 2 FI and CF parameters of Eu^{3+} at the C_s site of β -Ga₂O₃ crystals (in cm⁻¹)^{*a*}

Parameters	Values	Parameters	Values		
Eave	63 304(15)	P^2	360		
$ \begin{array}{c} E_{\rm avg} \\ F^2 \\ F^4 \end{array} $	81 280(57)	B_0^2	41(46)		
F^4	61 647(93)	B_2^2	-625(31)		
F^{6}	40 535	$B_0^2 \\ B_2^2 \\ B_0^4$	-988(48)		
ξ	1319(1)	Re B_2^4	-397(89)		
α	20.16	Im B_2^4	-1243(42)		
β	-567	Re B_4^4	-165(71)		
γ	1500	Im B_4^4	223(48)		
T^2	300	B_0^6	-1096(84)		
T^3	40	Re B_2^6	-177(78)		
T^4	60	Im $B_2^{\overline{6}}$	-201(59)		
T^6	-300	Re B_4^6	73(93)		
T^7	370	Im B_4^6	553(58)		
T^8	320	Re B_6^6	720(53)		
M^0	2.1	Im B_6^6	151(166)		
rms ^b	12.9	-	· · ·		

^{*a*} Values in parentheses are errors in the indicated parameters which are freely varied in the fit. ^{*b*} The root-mean-square (rms) deviation between the experimental and calculated energies was used as a figure of merit to describe the quality of a fit, with rms = $\sqrt{\sum (E_{exp} - E_{calc})^2/(N - P)}$, where N = 71, the number of CF levels fit, and P = 19, the number of parameters freely varied.

not only ionic radius but also other factors including optical electronegativity, covalency, and structural distortion could influence the CF strength of Eu^{3+} . For instance, in contrary to the M₂O₃ series, the CF strength of Eu^{3+} increases with increasing ionic radius of the host cations for LnOX series (Ln = Y, Gd, and La; X = Cl and Br).⁶⁰ The CF strengths of Eu³⁺ in various crystals have been summarized by Chen and Liu.⁶⁰ A relatively large *S* value can be found for Eu³⁺-doped β -Ga₂O₃ because RE ions occupying a lower site symmetry normally have a larger CF strength.

3.5 Luminescence lifetime

PL decays of the ${}^{5}D_{0}$ multiplet were measured at 10–300 K for the sample annealed at 1100 °C (Fig. 7). All the curves exhibit nearly single exponential behavior and the fitted PL lifetime is 0.939 ms at 10 K. No rising time in the initial part of the decay curves can be observed within the detectable limit, in accordance with the efficient host-to Eu3+ ET and multiphonon relaxation from upper multiplets to ${}^{5}D_{0}$. The inset of Fig. 7 shows the dependence of temperature on the PL lifetime of ${}^{5}D_{0}$ at 3–300 K determined by single exponential fit. It can be found that the PL lifetime increases significantly as the temperature decreases from 150 to 30 K, but only changes insignificantly below 20 K. Therefore, it is reasonable to regard the observed ${}^{5}D_{0}$ lifetime at 10 K (0.939 ms) as the intrinsic radiative lifetime of ${}^{5}D_{0}$ for Eu³⁺ in β -Ga₂O₃. Generally, the multiphonon nonradiative relaxation between ${}^{5}D_{0}$ and ${}^{7}F_{6}$ multiplets of Eu³⁺ in β -Ga₂O₃ can be neglected because the energy gap between them ($\sim 12000 \text{ cm}^{-1}$) is about 15 times the maximum phonon energy ($\sim 760 \text{ cm}^{-1}$) of β -Ga₂O₃.^{62,63} Thus it is expected that the ⁵D₀ lifetime of Eu³⁺ varies little with the temperature. Nevertheless the observed strong temperature-dependency of the ${}^{5}D_{0}$ lifetime

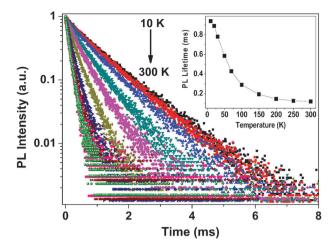


Fig. 7 PL decays from ${}^{5}D_{0}$ measured at 10–300 K by monitoring the ${}^{5}D_{0} \rightarrow {}^{7}F_{2}$ emission upon excitation at 266 nm for the sample annealed at 1100 °C. The inset shows the temperature dependence of the PL lifetime determined by single exponential fit.

(Fig. 7) indicates that a phonon-assisted nonradiative ET process could be the dominant nonradiative mechanism. Similar decay behaviors of ${}^{5}D_{0}$ were also observed in Eu³⁺ : BaFCl,⁶⁴ Cs₂NaEuCl₆,⁶⁵ EuAl₃B₄O₁₂,⁶⁶ EuMgB₅O₁₀,⁶⁷ $Eu_2(MoO_4)_{3}^{68}$ and Eu_2O_3 crystals.⁶⁹ The possible reasons for these unusual PL decay behaviors are due to: (1) ET from ${}^{5}D_{0}$ to the impurity ions or defects in those crystals; (2) ET between Eu³⁺ ions occupying different crystallographic sites. Herein we infer that reason (1) may play the key role since no multiplet Eu³⁺ sites were observed in our samples. The PL decay curves of the samples annealed at 650, 900 and 1000 °C at 10 K and RT were also measured, showing that they have nearly the same PL lifetimes as that of the sample annealed at 1100 °C. The PL lifetime of the sample annealed at lower temperature was expected to be shorter than that of the sample annealed at 1100 °C, in view of the existence of more defects such as oxygen vacancies in the sample annealed at lower temperature. However, the nearly same PL lifetime of different samples indicates that oxygen vacancies may not be the quenching centers of the Eu³⁺ luminescence. The origin of the impurity ions or crystal defects remains unclear and needs further investigation.

The theory of diagonal phonon-assisted ET processes was systematically formulated by Holstein *et al.*, and the approximate temperature-dependent ET rates for different microscopic mechanisms were summarized.^{64,70,71} The nonradiative ET rate ($W_{\rm NR}$) of Eu³⁺ in β -Ga₂O₃ at various temperatures was calculated based on the observed lifetimes ($\tau(T)$) using the formula $W_{\rm NR} = \tau(T)^{-1} - \tau_0^{-1}$, where τ_0 is the radiative lifetime (0.939 ms) of Eu³⁺, and plotted in Fig. 8. The data can be well fitted according to the two-phonon assisted one-site resonant process using the following equation:⁷²

$$W_{\rm NR} = A + B \exp(-\Delta/k_{\rm B}T), \qquad (5)$$

where Δ is the energy splitting to a real state and k_B is Boltzmann's constant. The fitted values are $1.39 \times 10^5 \text{ s}^{-1}$ for A, $1.31 \times 10^7 \text{ s}^{-1}$ for B, and 360 cm⁻¹ for Δ . For this

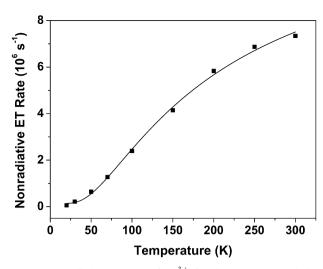


Fig. 8 Nonradiative ET rate of Eu^{3+} for the sample annealed at 1100 °C as a function of temperature. The scattering points are experimental data and the solid line denotes fitting results from eqn (5).

mechanism, a third electronic level near excited or ground state of donor ions is required. Obviously, for Eu³⁺ ions, the third level could be near the ground state (⁷F₀) since there is no such level in the proximity of ⁵D₀. The energy gap between ⁷F₀ and the second sub-level of ⁷F₁ is 401 cm⁻¹ in β-Ga₂O₃, which is close to 360 cm⁻¹ of Δ . Thus this CF level of ⁷F₁ may act as the third level in the above ET process. The same ET mechanism was also observed in Eu³⁺-to-Nd³⁺ and Eu³⁺-to-Ni²⁺ ET processes in EuMgB₅O₁₀ crystals.⁷²

4. Conclusions

The electronic structure and optical spectroscopy of Eu³⁺-doped β -Ga₂O₃ NCs, synthesized by a simple combustion method, have been systematically investigated. The evolution of optical spectra with increasing the annealing temperature of NCs shows unambiguously that more Eu³⁺ ions were incorporated into the crystal lattice with the growth of NCs. Eu³⁺ ions were found to occupy only a single lattice site despite of two nonequivalent Ga^{3+} sites in β -Ga₂O₃. Spectroscopic evidence revealed the local point-group symmetry of C_s for Eu³⁺ at this single site, and thus clarifies the previously controversial assignments. CF levels of Eu^{3+} at the C_s site with a total number of 71 have been identified and fitted in terms of 19 freely varied free-ions and CF parameters, which yielded a small standard deviation of 12.9 cm⁻¹. The Eu³⁺ in β -Ga₂O₃ experiences a large CF strength of 546 cm⁻¹, which is consistent with the relatively low site symmetry (C_s) of Eu^{3+} . PL decays of the ⁵D₀ multiplet for Eu^{3+} in the sample annealed at 1100 °C showed an unusual temperaturedependent behavior due probably to the ET from the excited Eu³⁺ to impurity ions or crystal defects. The nonradiative ET mechanism of Eu³⁺ involved may be dominated by the two-phonon assisted one-site resonant process, as evidenced by the dependence of temperature on the ET rate that obeys the function of $\exp(-\Delta/k_{\rm B}T)$. The intrinsic radiative lifetime of ${}^{5}D_{0}$ of Eu³⁺ in β -Ga₂O₃ was determined to be 0.939 ms. A comprehensive survey of electronic structure and optical

properties of Eu^{3+} in β -Ga₂O₃ nanophosphors is of crucial importance for their potential applications in the fields of optoelectronic devices, phosphors, biodetection or bio-imaging.

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